

Section:	1 – 8 Use Quadratic Formula and the Discriminant
Essential Question	How do you use the quadratic formula and the discriminant?

Key Vocab:

Quadratic Formula	Let a , b , and c be real numbers such that $a \neq 0$, then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ can be used to solve <u>ANY quadratic equation</u> in standard form $ax^2 + bx + c = 0$. (Sing the song “Pop Goes the Weasel” to remember the quadratic formula!)
Discriminant	Radicand of the quadratic formula: <u>$b^2 - 4ac$</u> .

Using the Discriminant:

Discriminant

The discriminant of the quadratic equation $ax^2 + bx + c = 0$ ($a \neq 0$) is $b^2 - 4ac$.

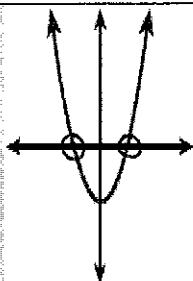
$$b^2 - 4ac > 0$$

$$b^2 - 4ac = 0$$

$$b^2 - 4ac < 0$$

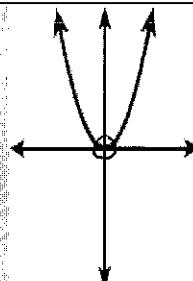
Discriminant is positive

TWO REAL ROOTS



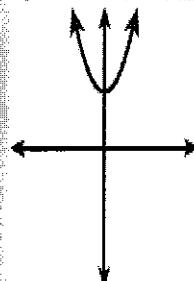
Discriminant is zero

ONE REAL ROOT



Discriminant is negative

TWO IMAGINARY ROOTS



Show:

Ex 1: Use the quadratic formula to solve.

$$\begin{aligned} a &= 1 \\ b &= -5 \\ c &= -7 \end{aligned}$$

Quad. Formula

$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(-7)}}{2(1)}$$

$$x = \frac{5 \pm \sqrt{25 + 28}}{2}$$

$$x = \boxed{\frac{5 \pm \sqrt{53}}{2}}$$

$$b. \quad x^2 - 6x + 10 = 0$$

$$a = 1$$

$$b = -6$$

$$c = 10 \quad \text{Quad. Formula}$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(10)}}{2(1)}$$

$$x = \frac{6 \pm \sqrt{36 - 40}}{2}$$

$$x = \frac{6 \pm \sqrt{-4}}{2} = \frac{6 \pm \sqrt{4}i}{2}$$

$$x = \frac{6 \pm 2i}{2} = \boxed{3 \pm i}$$

$$c. \quad 16x^2 - 23x = 17x - 25$$

$$\underline{+25 \quad -17x \quad -17x \quad +25}$$

$$16x^2 - 40x + 25 = 0$$

$$a = 16$$

$$b = -40$$

$$c = 25 \quad \text{Quad. Formula}$$

$$x = \frac{-(-40) \pm \sqrt{(-40)^2 - 4(16)(25)}}{2(16)}$$

$$x = \frac{40 \pm \sqrt{1600 - 1600}}{32} = \frac{40 \pm 0}{32}$$

$$x = \frac{40}{32} = \boxed{\frac{5}{4}}$$

Ex 2: Find the discriminant of the quadratic equation. Use the discriminant to determine the number of solutions for the equation.

$$a. \quad x^2 + 10x + 23 = 0$$

$$D = b^2 - 4ac$$

$$a = 1$$

$$b = 10$$

$$c = 23$$

$$D = (10)^2 - 4(1)(23)$$

$$D = 100 - 92$$

$$\boxed{D = 8}$$

(positive)

TWO REAL ROOTS

$$b. \quad x^2 + 10x + 25 = 0$$

$$a = 1 \quad D = b^2 - 4ac$$

$$b = 10 \quad D = (10)^2 - 4(1)(25)$$

$$c = 25$$

$$D = 100 - 100$$

$$\boxed{D = 0}$$

(zero)

ONE REAL ROOTS

$$c. \quad x^2 + 10x + 27 = 0$$

$$a = 1 \quad D = b^2 - 4ac$$

$$b = 10$$

$$c = 27 \quad D = (10)^2 - 4(1)(27)$$

$$D = 100 - 108$$

$$\boxed{D = -8}$$

(negative)

TWO IMAGINARY ROOTS

Ex 3: For an object that is launched or thrown the equation $h = -16t^2 + v_0t + h_0$, where v_0 stands for an initial velocity and h_0 stands for the initial height. A basketball player passes the ball to a teammate. The ball leaves the player's hand 5 feet above the ground and has an initial vertical velocity of 55 feet per second. The teammate catches the ball when it returns to a height of 5 feet. How long is the ball in the air?

$$h = -16t^2 + v_0t + h_0$$

$$\begin{array}{r} 5 = -16t^2 + 55t + 5 \\ -5 \end{array}$$

$$0 = -16t^2 + 55t + 0$$

$$a = -16$$

$$b = 55$$

$$c = 0$$

Quad. Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-55 \pm \sqrt{3025 - 0}}{-32} = \frac{-55 \pm \sqrt{3025}}{-32}$$

$$x = \frac{-55 \pm 55}{-32}$$

$$x = \frac{-55 + 55}{-32} = \frac{0}{-32} = 0 \text{ seconds}$$

$$x = \frac{-55 - 55}{-32} = \frac{-110}{-32} = 3.4 \text{ seconds}$$