

SHOW ALL WORK!

Evaluate the expression.

1. $4^{-6} \cdot 4^{-1}$

$$4^{-7} = \boxed{\frac{1}{4^7}}$$

2. $\left(\frac{2}{3}\right)^3$

$$\boxed{\frac{2^3}{3^3} \text{ or } \frac{8}{27}}$$

3. $(5^{-2})^2$

$$5^{-4} = \boxed{\frac{1}{5^4}}$$

Write the answer in scientific notation.

4. $(3.4 \times 10^{-1})(3.1 \times 10^{-2})$

$$10.54 \times 10^{-3}$$

$$\boxed{1.054 \times 10^{-2}}$$

5. $\frac{8.4 \times 10^{-6}}{2.4 \times 10^9}$

$$\boxed{3.5 \times 10^{-15}}$$

Simplify the expression

6. $\frac{y^4}{y^{-7}}$

$$y^{(4-(-7))} = \boxed{y^{11}}$$

7. $(2m^3n^{-1})(8m^4n^{-2})$

$$16m^{(3+4)}n^{(-1+(-2))}$$

$$16m^7n^{-3}$$

$$\boxed{\frac{16m^7}{n^3}}$$

8. $\frac{8e^{-4}f^{-2}}{18ef^{-5}}$

$$\frac{4e^{(-4-1)}f^{(-2-(-5))}}{9}$$

$$\frac{4e^{-5}f^3}{9} = \boxed{\frac{4f^3}{9e^5}}$$

Decide whether the function is a polynomial function. If it is, write the function in standard form and state the degree, type, and leading coefficient.

9. $g(x) = \pi - 4x^2 + \frac{2}{x}$

Not a

~~polynomial~~ polynomial function

~~because~~ (negative exponent)

$$\frac{2}{x} = 2x^{-1}$$

~~not a polynomial~~

~~because~~

10. $h(x) = x^4 - x^3$

yes, polynomial function

stand. form: $x^4 - x^3$

degree: 4

type: quartic

lead. coeff.: 1

Describe the end behavior of the graph of the polynomial function by completing these statements: $f(x) \rightarrow \underline{\quad? \quad}$ as $x \rightarrow -\infty$ and $f(x) \rightarrow \underline{\quad? \quad}$ as $x \rightarrow +\infty$. **AND JUSTIFY.**

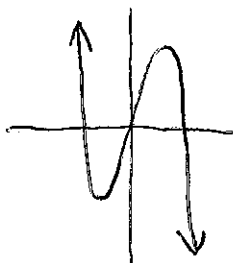
11. $f(x) = -x^7 + 10x$

As $x \rightarrow -\infty$

$f(x) \rightarrow \infty$

As $x \rightarrow \infty$

$f(x) \rightarrow -\infty$



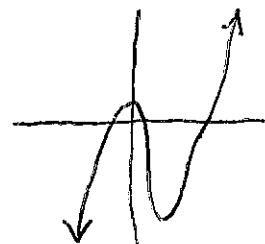
12. $f(x) = 2x^5 - 7x^2 - 4x$

As $x \rightarrow -\infty$

$f(x) \rightarrow -\infty$

As $x \rightarrow \infty$

$f(x) \rightarrow \infty$



Find the sum or difference.

13. $(2y^2 - 5y + 1) + (y^2 - y - 4)$

$(2y^2 + y^2) + (-5y - y) + (1 - 4)$

$3y^2 - 6y - 3$

14. $(10v^4 - 2v^2 + 6v^3 - 7) - (9 - v + 2v^4)$

$10v^4 - 2v^2 + 6v^3 - 7 - 9 + v - 2v^4$

$(10v^4 - 2v^4) + (6v^3) + (-2v^2) + (v) + (-7 - 9)$

$8v^4 + 6v^3 - 2v^2 + v - 16$

Find the product.

15. $(x - 3)^2$

$(x - 3)(x - 3)$

$x^2 - 6x + 9$

16. $(n + 5)(2n^2 - n - 7)$

$2n^3 - n^2 - 7n$
 $+ 10n^2 - 5n - 35$

$2n^3 + 9n^2 - 12n - 35$

17. $(2f + 1)^3$

$(2f + 1)(2f + 1)(2f + 1)$

$(4f^2 + 2f + 2f + 1)(2f + 1)$

$(4f^2 + 4f + 1)(2f + 1)$

$8f^3 + 4f^2$

$+ 8f^2 + 4f$

$+ 2f + 1$

$8f^3 + 12f^2 + 6f + 1$

$8f^3 + 12f^2 + 6f + 1$

Factor the polynomial completely using any method.

18. $x^3 + 125$

Sum of cubes
 $a = x \quad b = 5$

$(x + 5)(x^2 - 5x + 25)$

19. $(x^3 + 6x^2) + (7x + 42)$

$x^2(x + 6) + 7(x + 6)$

$(x^2 + 7)(x + 6)$

factoring
by
grouping

20. $c^4 - 81$

diff. of squares

$(c^2 + 9)(c^2 - 9)$

$(c^2 + 9)(c + 3)(c - 3)$

Find all the zeros of the polynomial function.

21. $h(x) = 2x^4 + x^3 + x^2 + x - 1$ ↖ degree 4 = 4 solutions

① Poss. Rat. Zeros

C: -1
Factors: 1 $\frac{C}{LC} = \pm \frac{1}{1}, \pm \frac{1}{2}$
LC: 2
Factors: 1, 2

② Check calculator table for real zeros

$x = -1, \frac{1}{2}$

③
$$\begin{array}{r|rrrrrr} -1 & 2 & 1 & 1 & 1 & -1 \\ & \downarrow & -2 & 1 & -2 & 1 \\ \hline \frac{1}{2} & 2 & -1 & 2 & -1 & 0 \\ & \downarrow & 1 & 0 & 1 & \\ \hline & 2 & 0 & 2 & 0 & \end{array}$$

⑤ $2x^2 + 0x + 2 = 0$

$2x^2 + 2 = 0$
 $-2 \quad -2$

$\frac{2x^2}{2} = \frac{-2}{2} \quad \sqrt{x^2} = \sqrt{-1} \quad x = \pm i$

⑥ Zeros = $-1, \frac{1}{2}, \pm i$

Determine the possible numbers of positive real zeros, negative real zeros, and imaginary zeros for the function.

23. $g(x) = x^4 + 3x^2 - 10x + 16$

Positive Zeros (2 sign changes)

2
0

Negative Zeros

0

$g(-x) = (-x)^4 + 3(-x)^2 - 10(-x) + 16$
 $g(-x) = x^4 + 3x^2 + 10x + 16$
(0 sign changes)

Imaginary Zeros

2

4

degree = 4 → 4 solutions/zeros

$2 + 0 = 2 \quad 4 - 2 = 2$

$0 + 0 = 0 \quad 4 - 0 = 4$

24. $f(x) = x^6 + 2x^5 - 12x^4 - x^3 + 7x^2 + 5x - 16$

Positive Zeros

3
1

Negative Zeros

3
1

$f(-x) = (-x)^6 + 2(-x)^5 - 12(-x)^4 - (-x)^3 + 7(-x)^2 + 5(-x) - 16$
 $+5(-x) - 16$

$f(-x) = x^6 - 2x^5 - 12x^4 + x^3 + 7x^2 - 5x - 16$
(3 sign changes)

Imaginary

0
2
4

degree = 6 → 6 zeros

$3 + 3 = 6 \quad 6 - 0 = 6$

$3 + 1 = 4 \quad 6 - 4 = 2$

$1 + 3 = 4 \quad 6 - 4 = 2$

$1 + 1 = 2 \quad 6 - 2 = 4$

Write a polynomial function f of least degree that has rational coefficients, a leading coefficient of 1, and the given zeros.

25. $4+i, 0$

$$(x - (4+i))(x - (4-i))(x)$$

$$(x - 4 - i)(x - 4 + i)(x)$$

$$(x^2 - 4x + ix - 4x + 16 - 4i + 4i - i^2)(x)$$

$$(x^2 - 4x - 4x + 16 - (-1))(x)$$

$$(x^2 - 8x + 17)x$$

$$f(x) = x^3 - 8x^2 + 17x$$

26. $-3, 0, 1$

$$(x+3)(x)(x-1)$$

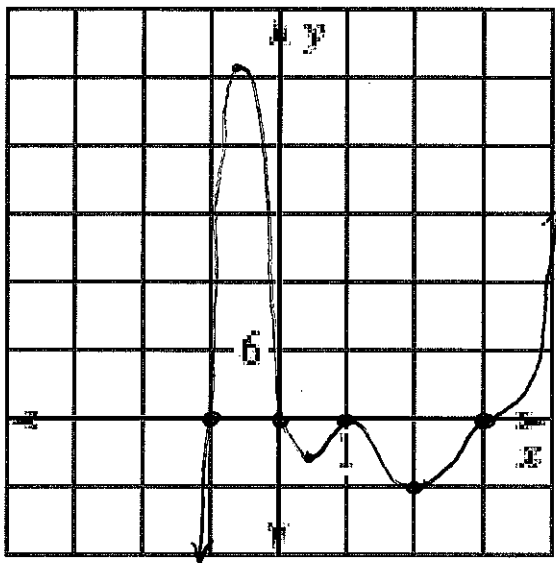
$$(x^2 + 3x)(x-1)$$

$$x^3 - x^2 + 3x^2 - 3x$$

$$f(x) = x^3 + 2x^2 - 3x$$

Use a graphing calculator to graph the function. (Be sure to label all x -intercepts, local maximums, and local minimums)

7. 27. $g(x) = x(x+1)(x-1)^2(x-3)^3$



x -intercepts: $(0,0)$ $(-1,0)$ $(1,0)$ $(3,0)$

local max: $(-0.7, 30.7)$

local min: $(2.3, -3.8)$ $(2, -6)$